International macroeconomics Collection of formulas

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1 Balance sheets

Households	Assets		Liabilities	
	Money	[1], [2]	Net wealth	
	Bonds, shares	[3], [4]	Loans from banks	[5]
	Real assets			
Firms	Assets		Liabilities	
	Money	[1], [2]	Equity	[4]
	Bonds, shares	[3], [4]	Loans from banks	[6]
	Real assets		Corporate bonds [3]	
Covernment	Assats		Lishilities	
Government	ASSELS		Liabilities	
	Money	[1], [2]	Net wealth	
	Bonds, shares	[3], [4]	Government bonds	
	Real assets			
Banks	Assets		Liabilities	
	Bank notes and coins	[1]	Equity	[4]
	Bank reserves	[8]	Bonds	[3]
	Bank loans to households	[5]	Bank deposits	[2]
	Bank loans to firms	[6]		
Central bank	Assets		Liabilities	
	Domestic credit	[3]	Bank reserves	[8]
	Official reserves	[7]	Bank notes and coins	[1]

Table 1: Balance sheets of economic agents.

Home economy	Assets		Liabilities	
	Bank notes and coins Bank reserves Real assets Net foreign assets (excl. CB)	[1] [8]	Domestic real wealth Net external wealth (excl. CB) Domestic credit	[3]
Home central bank	Assets		Liabilities	
	Domestic credit Domestic official reserves	[3] [7]	Bank reserves Bank notes and coins	[8] [1]

Table 2: Consolidated balance sheets of home economy and central bank.

Home country	Assets	Liabilities	
	Real assets	Domestic real wealth	
	Net foreign assets	Net external wealth	

Table 3: Consolidated balance sheet of home country.

Households	Assets		Liabilities	
	Money	[1] [2]	Net wealth	
	Bonds, shares	[1], [2] [3], [4]	Loans from banks	
	Real assets	[-],[.]		[-]
Firms	Assets	Liabilities		
	Money	[1], [2]	Equity	[4]
	Bonds, shares	[3], [4]	Loans from banks	[6]
	Real assets		Corporate bonds	[3]
Government	Assets		Liabilities	
	Money	[1], [2]	Net wealth	
	Bonds, shares	[3], [4]	Government bonds	[3]
	Real assets			
Banks	Assets		Liabilities	
	Bank notes and coins	[1]	Equity	[4]
	Bank reserves	[8]	Bonds	[3]
	Bank loans to households	[5]	Bank deposits	
	Bank loans to firms	[6]		
Central bank	Assets		Liabilities	
	Domestic credit	[3]	Bank reserves	[8]
	Official reserves	[7]	Bank notes and coins	[1]
Home economy	Assets		Liabilities	
	Bank notes and coins	[1]	Domestic real wealth	
	Bank reserves	[8]	Net external wealth (excl. CB)	
	Real assets	[*]	Domestic credit	[3]
	Net foreign assets (excl. CB)			
Home central bank	Assets		Liabilities	
	Domestic credit	[3]	Bank reserves	[8]
	Domestic official reserves	[7]	Bank notes and coins	[1]
Home country	Assets		Liabilities	
	Real assets		Domestic real wealth	
	Net foreign assets		Net external wealth	

Table 4: Balance sheet summary.

2 Exchange rates

Eq. no.	Equation or formula	In logarithms	Equiv- alence	Туре	Economic interpretation	Economic justification
1	P^{H}	$p^{\scriptscriptstyle \mathrm{H}}$		Definition	Domestic price level	
2	P^{F}	$p^{ extsf{F}}$		Definition	Foreign price level	
3	S	8		Definition	Nominal exchange rate (foreign-currency price of domestic currency)	
4	$Q = \frac{SP^{\rm H}}{P^{\rm F}}$	$q = s + p^{\rm H} - p^{\rm F}$		Definition	Real exchange rate (ratio of domestic and foreign price level, where both price levels are converted to the same currency)	
5	$\frac{1}{P^{\mathrm{H}}}$	$-p^{^{\mathrm{H}}}$		Definition	Purchasing power of domestic currency at home	
6	$rac{S}{P^{\mathrm{F}}}$	s - pF		Definition	Purchasing power of domestic currency abroad	
7	$\frac{1}{SP^{\text{H}}}$	$-s - p^{\mathrm{H}}$		Definition	Purchasing power of foreign currency at home	
8	$\frac{1}{P^{F}}$	$-p^{\mathrm{F}}$		Definition	Purchasing power of foreign currency abroad	
9	$\pi^{\mathrm{H}}_t = \frac{P^{\mathrm{H}}_t - P^{\mathrm{H}}_{t-1}}{P^{\mathrm{H}}_{t-1}}$	$\pi^{\rm H}_t = \Delta p^{\rm H}_t$		Definition	Domestic inflation (in percent)	
10	$\pi^{\mathrm{F}}_t = \frac{P^{\mathrm{F}}_t - P^{\mathrm{F}}_{t-1}}{P^{\mathrm{F}}_{t-1}}$	$\pi^{\rm F}_t = \Delta p^{\rm F}_t$		Definition	Foreign inflation (in percent)	
11	$\frac{S_t - S_{t-1}}{S_t}$	Δs_t		Definition	Nominal appreciation (in percent)	
12	$\frac{Q_t - Q_{t-1}}{Q_t}$	Δq_t		Definition	Real appreciation (in percent)	

13	Q = 1	q = 0	13-17	Theory	Purchasing power parity (PPP)	Good market arbitrage: $Q > 1 \Rightarrow D^{H} \downarrow, D^{F} \uparrow \Rightarrow P^{H} \downarrow$ $, P^{F} \uparrow \Rightarrow Q \downarrow \Rightarrow Q = 1$
14	$P^{\rm H} = \frac{1}{S} P^{\rm F}$	$p^{\rm H}=-s+p^{\rm F}$	13-17	Theory	Equality of domestic and foreign good prices, both being expressed in the domestic currency (\Leftrightarrow PPP)	Good market arbitrage
15	$SP^{\rm H} = P^{\rm F}$	$s + p^{H} = p^{F}$	13-17	Theory	Equality of domestic and foreign good prices, both being expressed in the foreign curreny (\Leftrightarrow PPP)	Good market arbitrage
16	$\frac{1}{P^{\rm H}} = S \frac{1}{P^{\rm F}}$	$-p^{\mathrm{H}} = s - p^{\mathrm{F}}$	13-17	Theory	Equality of purchasing powers of domestic currency at home and abroad (PPP)	Good market arbitrage
17	$\frac{1}{SP^{\rm H}} = \frac{1}{P^{\rm F}}$	$-s - p^{H} = -p^{F}$	13-17	Theory	Equality of purchasing powers of foreign currency at home and abroad (PPP)	Good market arbitrage
18	$S = \frac{1/P^{\rm H}}{1/P^{\rm F}}$	$s = -(p^{\rm H} - p^{\rm F})$		Theory	Nom. exchange rate in basic model (implying PPP)	Currency conversions without effect on purchasing power
19	$S = \frac{1/P^{\mathrm{H}}}{1/P^{\mathrm{F}}} \!\times\! e^{\xi m^{\mathrm{HF}}}$	$s = -(p^{\rm H} - p^{\rm F}) + \xi m^{\rm HF}$	19-20	Theory	Nom. exchange rate in currency flow model	Net foreign money holdings \Rightarrow net currency market pressure
20	$Q=e^{\xi m^{\rm HF}}$	$q=\xi m^{\rm HF}$	19-20	Theory	Purchasing power parity fallacy (Eleftheriou and Müller-Plantenberg, 2018a,b): Real exchange rate proportional to currency market pressure, but independent of price levels	Combination of equations 4 and equation 19: Good market arbitrage \Rightarrow price level convergence offset by purchasing power divergence \Rightarrow no effect on real exchange rate

References

- Eleftheriou, Maria and Nikolas A. Müller-Plantenberg. Price level convergence and purchasing power divergence. *International Finance*, vol. 21, no. 1, 2018a, 71–91.
- Eleftheriou, Maria and Nikolas A. Müller-Plantenberg. The purchasing power parity fallacy: Time to reconsider the PPP hypothesis. *Open Economies Review*, vol. 29, no. 3, 2018b, 481–515.